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# Switched Capacitive Filter for Harmonic Suppression in Variable Speed Induction Motor Drives

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# Outline

- ▶ Motivation
- ▶ Eliminating 5<sup>th</sup> and 7<sup>th</sup> order harmonics
- ▶ Problems to be addressed
- ▶ Capacitive filtering - Ensuring an inverter to contribute zero active power
- ▶ Proposed Solution
- ▶ Experimental Results
- ▶ Related work done
- ▶ Summary
- ▶ Publications

# Motivation

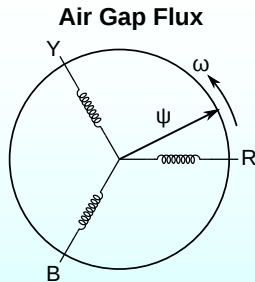
## Effect of 5th and 7th order harmonics on Induction Motors

➔ Fundamental

$$V_{R1} = V_1 \sin \omega t$$

$$V_{Y1} = V_1 \sin(\omega t + 120^\circ)$$

$$V_{B1} = V_1 \sin(\omega t - 120^\circ)$$



# Motivation

## Effect of 5th and 7th order harmonics on Induction Motors

### ➔ Fundamental

$$V_{R1} = V_1 \sin \omega t$$

$$V_{Y1} = V_1 \sin(\omega t + 120^\circ)$$

$$V_{B1} = V_1 \sin(\omega t - 120^\circ)$$

### ➔ 5<sup>th</sup> Harmonic

$$V_{R5} = V_5 \sin 5\omega t$$

$$V_{Y5} = V_5 \sin\{5(\omega t + 120^\circ)\}$$
$$= V_5 \sin(5\omega t - 120^\circ)$$

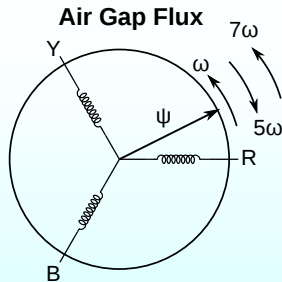
$$V_{B5} = V_5 \sin\{5(\omega t - 120^\circ)\}$$
$$= V_5 \sin(5\omega t + 120^\circ)$$

### ➔ 7<sup>th</sup> Harmonic

$$V_{R7} = V_7 \sin 7\omega t$$

$$V_{Y7} = V_7 \sin\{7(\omega t + 120^\circ)\}$$
$$= V_7 \sin(7\omega t + 120^\circ)$$

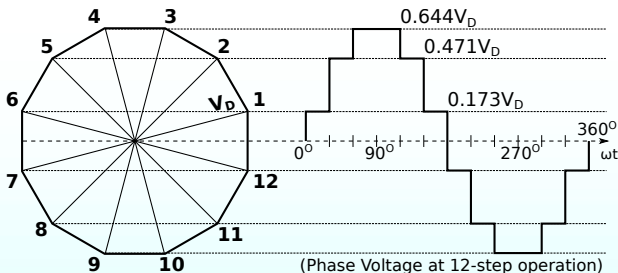
$$V_{B7} = V_7 \sin\{7(\omega t - 120^\circ)\}$$
$$= V_7 \sin(7\omega t - 120^\circ)$$



**6<sup>th</sup> Harmonic flux ripple over the fundamental, resulting in torque ripple**

# Eliminating 5th and 7th order harmonics

## 12-sided Voltage Space Vectors(VSV)



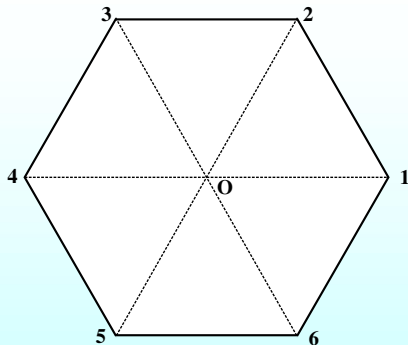
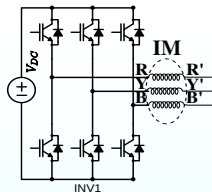
$$V_{phase,n} = \frac{4}{\pi} \int_0^{\frac{\pi}{2}} V_{phase} \sin(n\omega t) d\omega t$$

$$V_{phase,n} = \frac{4V_d}{n\pi} \left[ 0.173 + 0.298 \cos\left(\frac{n\pi}{6}\right) + 0.173 \cos\left(\frac{n\pi}{3}\right) \right]$$

$$\mathbf{V}_{phase,1} = 0.659V_d; \mathbf{V}_{phase,5} = \mathbf{V}_{phase,7} = \mathbf{V}_{phase,17} = \mathbf{V}_{phase,19} = 0$$

# Eliminating 5th and 7th order harmonics

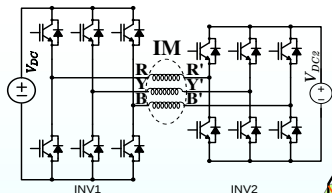
Generating 12-sided VSV



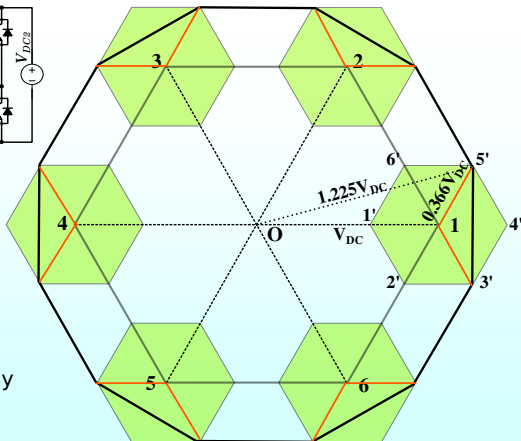
- Two-level inverter feeding star connected 3-phase IM
- Hexagonal space vector structure
- Higher switching frequency required for harmonic suppression
- Bulky passive line filters required for harmonic suppression

# Eliminating 5th and 7th order harmonics

## Generating 12-sided VSV



- Second inverter feeding from other end of IM winding terminals
- 12-sided space vector structure
- Multiple DC power supply ( $V_{DC}$ ,  $0.366V_{DC}$ )



K. K. Mohapatra, K. Gopakumar, V. T. Somasekar, and L. Umanand, "A harmonic elimination and suppression scheme for an open-end winding induction motor drive," IEEE Trans. Ind. Electron., vol. 50, no. 6, pp. 1187-1198, Dec. 2003.

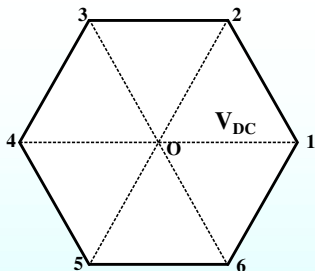
# Problems to be addressed

- ▶ Eliminating 5<sup>th</sup> and 7<sup>th</sup> order harmonics for the full speed range of the induction motor
- ▶ Avoiding multiple DC supplies
- ▶ Avoiding bulky passive line filters
- ▶ Avoiding any offline computation and requirement for look-up tables (required in Selective Harmonic Elimination)
- ▶ Shifting high frequency switching to low voltage stress devices
- ▶ Increasing the linear modulation range of the inverter

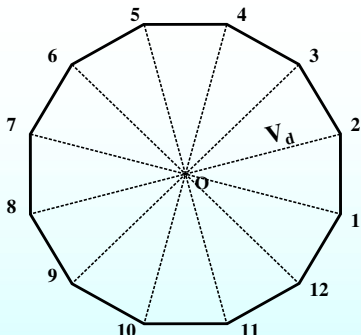


# Capacitive Filtering

Ensuring Zero Active Power by Inverter-2



Peak fundamental voltage  
for six-step operation=  
 **$0.637V_{DC}$**



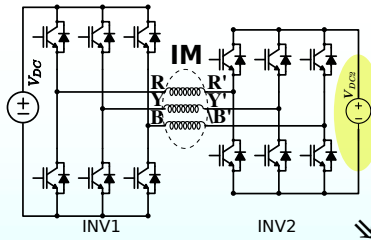
Peak fundamental voltage  
for twelve-step operation=  
 **$0.659V_d$**

**Equal fundamental voltage  $\Rightarrow$  Equal active power generation**

$$V_d = 0.966V_{DC}$$

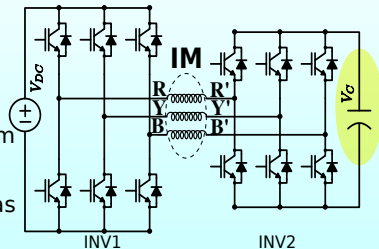
# Proposed Solution

## Power Circuit



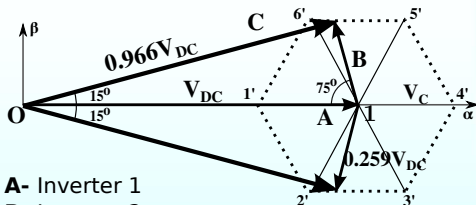
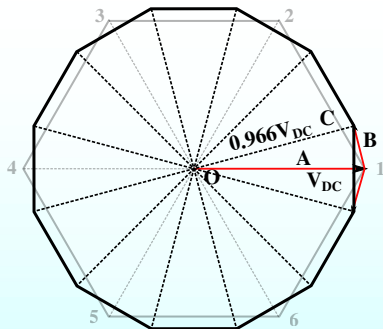
- Multiple power supply
- Active power contribution from the secondary inverter

- DC supply of secondary inverter substituted by capacitor
- No active power contribution from secondary inverter
- Capacitor fed inverter operates as filter



# Proposed Solution

## Vector Construction



- A- Inverter 1
- B- Inverter 2

### Extreme point in linear modulation range

$$V_{\text{phase, pk}} = (2/3)(0.966 V_{\text{DC}} \cos 15^\circ) = \mathbf{0.622 V_{\text{DC}}}$$

Extreme linear modulation supply frequency =

**48.8Hz**

Increase in linear modulation range (%) =

**7.8%**

$$16' k T_1 + 15' (1-k) T_1 = B T_1$$

$$\Rightarrow V_C \angle -60^\circ k T_1 + V_C \angle 60^\circ (1-k) T_1$$

$$= 0.259 V_{\text{DC}} \angle -75^\circ T_1 \quad (1)$$

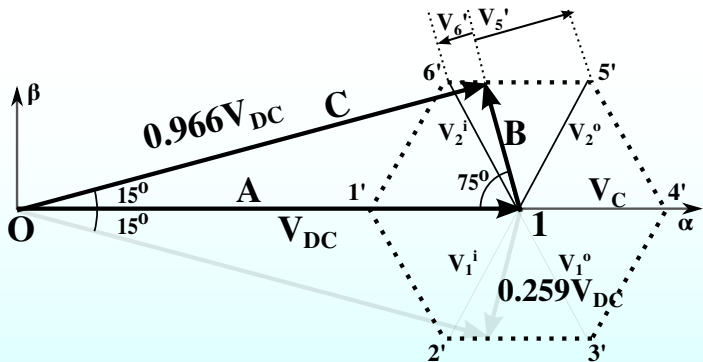
Resolving Eq. 1 in  $\alpha$ - $\beta$  axes:

$$V_C = \mathbf{0.289 V_{\text{DC}}}$$

$$k = \mathbf{0.732}$$

# Proposed Solution

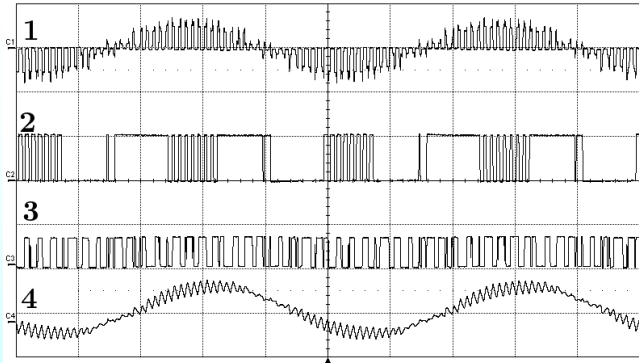
## Capacitor Voltage Control



- $V_{6'}$  and  $V_{5'}$  having opposing effect on the capacitor for a particular load current direction
- Capacitor voltage controlled by controlling duty ratio  $k$

# Experimental Results

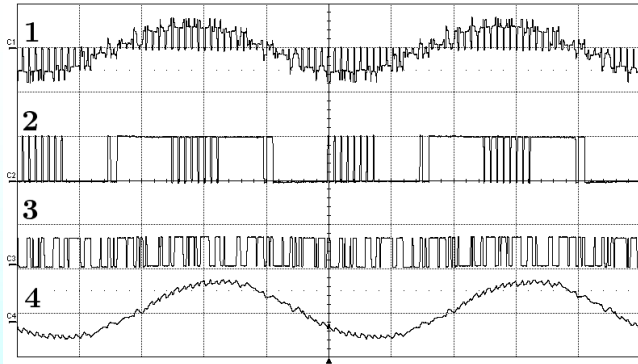
20Hz



- 1.** Phase Voltage-(200V/div), **2.** Inv-1 Pole Voltage-(200V/div)  
**3.** Inv-2 Pole Voltage-(100V/div), **4.** Phase current-1A/div.  
**X-axis:** 10ms/div

# Experimental Results

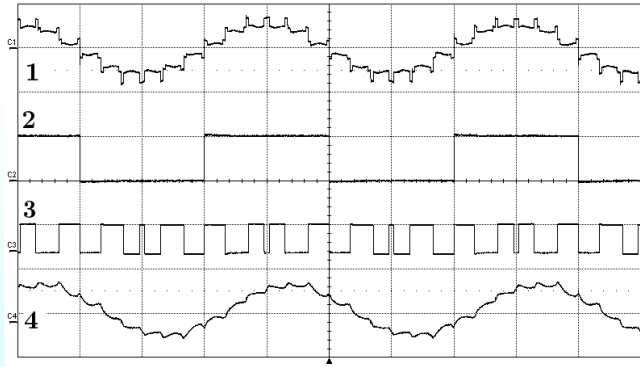
40Hz



- 1.** Phase Voltage-(200V/div), **2.** Inv-1 Pole Voltage-(200V/div)  
**3.** Inv-2 Pole Voltage-(100V/div), **4.** Phase current-1A/div.  
**X-axis:** 5ms/div

# Experimental Results

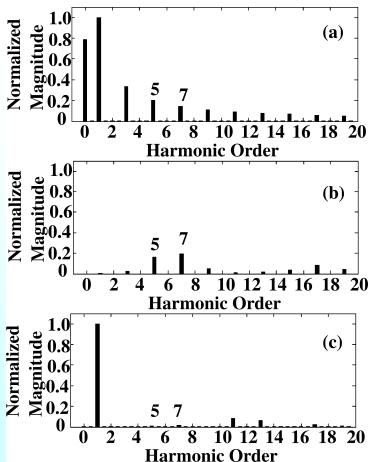
50Hz



- 1.** Phase Voltage-(200V/div), **2.** Inv-1 Pole Voltage-(200V/div)  
**3.** Inv-2 Pole Voltage-(100V/div), **4.** Phase current-1A/div.  
**X-axis:** 5ms/div

# Experimental Results

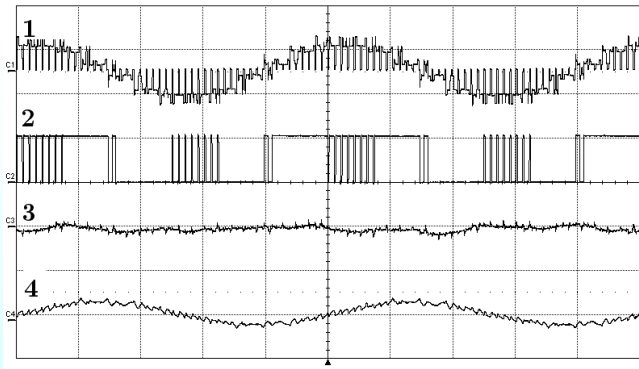
50Hz





# Experimental Results

## Capacitor Ripple at 40Hz

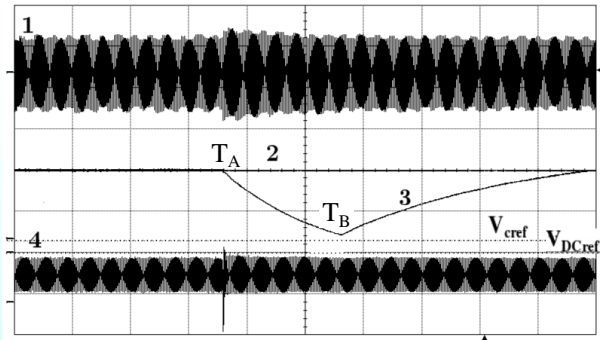


- 1.** Phase Voltage-(200V/div), **2.** Inv-1 Pole Voltage-(200V/div)  
**3.** Capacitor Ripple voltage-(5V/div), **4.** Phase current-2A/div.  
**X-axis:** 5ms/div

# Experimental Results

## Capacitor Control at 40Hz

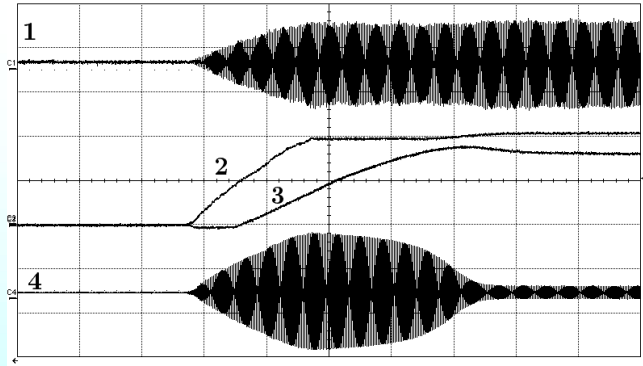
$T_A$  voltage controller reset;  $T_B$  controller switched ON



1. Phase Voltage-(50V/div), 2. DC-Bus Voltage-(50V/div)
  3. Capacitor voltage-(20V/div), 4. Phase current-0.5A/div.
- X-axis: 1s/div**

# Experimental Results

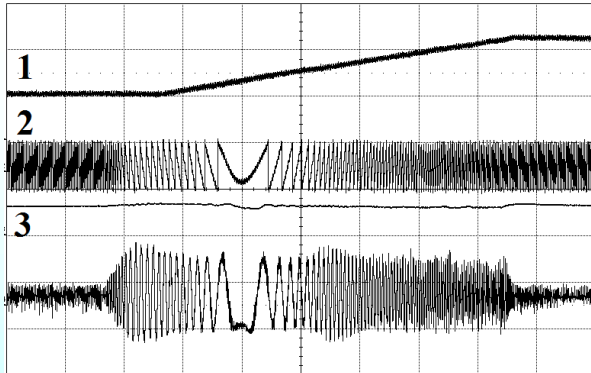
Starting Transients at 40Hz



- 1. Phase Voltage-(50V/div), 2. DC-Bus Voltage-(50V/div)
  - 3. Capacitor voltage-(20V/div), 4. Phase current-2A/div.
- X-axis: 1s/div**

# Experimental Results

Vector Control Speed Reversal (-48Hz - 48Hz)



**1: Machine speed(2500rpm/div), 2: Rotor position(6.28rad/div)**  
**3: Filter capacitor voltage(100V/div), 4: Phase Current(2A/div)**  
Timescale: 1s/div

# Experimental Results

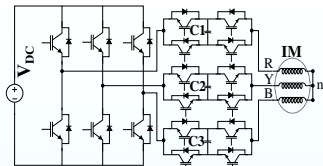
## Switching Frequency Comparison between Inverters

Frequency(Hz)	Switching Frequency(Hz)	
	Inverter-1	Inverter-2
10	180	360
20	360	720
30	540	1080
40	720	1440

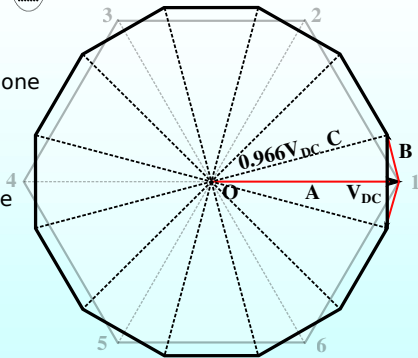
- ▶ Higher switching frequency required in conventional 2-level inverter to **suppress**  $6n \pm 1$  order harmonics
- ▶ Voltage stress across switches of secondary inverter is almost one third of that of primary inverter.

# Related Work Done

## Capacitive Filtering for Star Connected Induction Motor

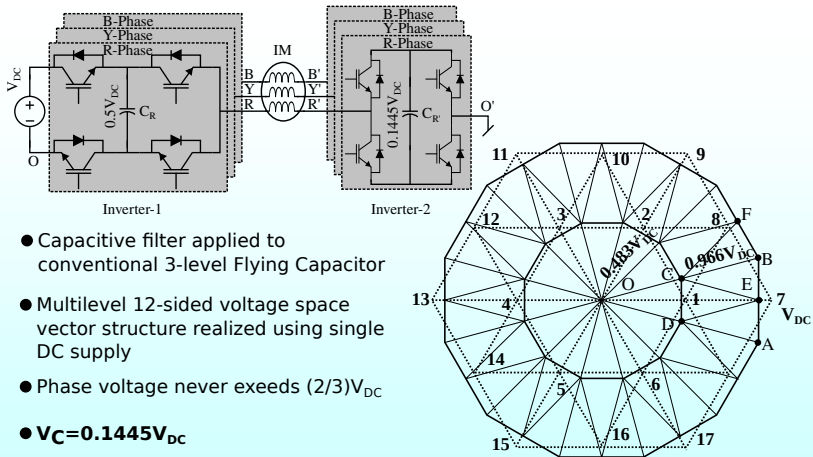


- Capacitors brought to one end of the motor
- **A** vector applied from 2-level inverter
- **B** vector applied by the cascaded H-bridges
- Phase voltage never exceeds  $(2/3)V_{DC}$
- $V_C = 0.1445V_{DC}$



# Related Work Done

## Capacitive Filtering Applied to form 3-level 12-sided VSV



# Summary

- ▶ Dodecagonal voltage space vector realized using single DC supply
- ▶ Complete elimination of the 5<sup>th</sup> and 7<sup>th</sup> order harmonics for the full speed range of the drive, including six-step operation of the primary inverter
- ▶ Increase in linear modulation range (45.3Hz to 48.8Hz)
- ▶ Higher switching frequency shifted to low voltage switches resulting in lesser switching loss
- ▶ No pre-charging circuitry required for the capacitor. Capacitor voltage inherently controlled by the PWM
- ▶ Proposed capacitive filtering scheme has been tested with rotor field oriented vector control with tight capacitor voltage control



- ▶ S. Pramanick, N. Abdul Azeez, S. Kaarthik, K. Gopakumar, and C. Cecati, "Low order harmonic suppression for open-end winding IM with dodecagonal space vector using a single dc-link supply", *IEEE Trans. Ind. Electron.*, vol. 62, issue 99, pp. 5340-5347, 2015.
- ▶ S. Pramanick, S. Kaarthik, N. Abdul Azeez, K. Gopakumar, S. Williamson and K. Rajashekara, "A Harmonic Suppression Scheme for Full Speed Range of a Two Level Inverter Fed Induction Motor Drive using Switched Capacitive Filter", *IEEE Trans. Power Electron.*, 2016
- ▶ S. Pramanick, M. Boby, N. Abdul Azeez, K. Gopakumar and S. Williamson, "A 3-Level Dodecagonal Space Vector based Harmonic Suppression Scheme for Open-End Winding IM Drives with Single DC Supply," *IEEE Trans. Ind. Electron.*, vol. PP, no. 99, pp. 11, 2016.



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# THANK YOU