

# A Novel Generalized Analytical Framework to Diagnose True Radial and Axial Displacements in an Actual Transformer Winding

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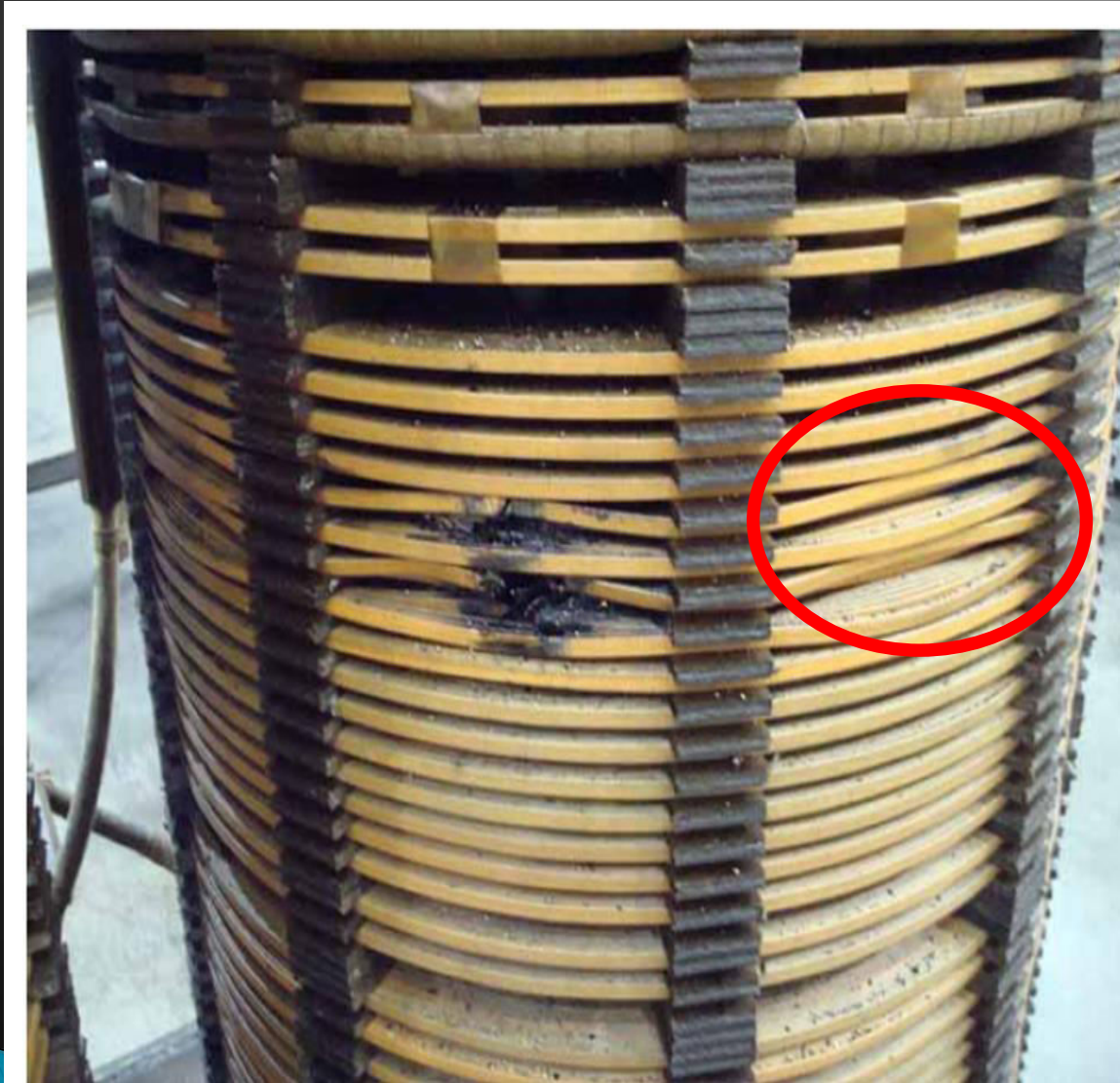
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# Typical failures : Nascent stage

If the damage in the nascent stage is allowed to grow, it may develop into a catastrophic failure in future.

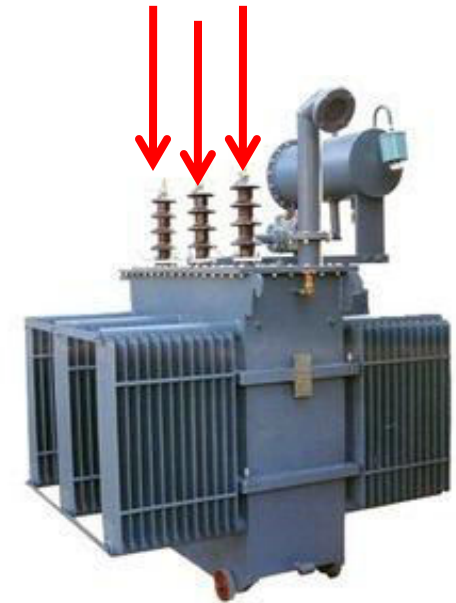
Thus, early detection of mechanical damage condition is paramount.



# Objectives

1. Damage-condition be identified at its infancy
2. Its location and severity should be assessable
3. Accomplish the above task non-invasively, i.e., using ONLY quantities that are measurable from the terminals

Terminals  
accessible

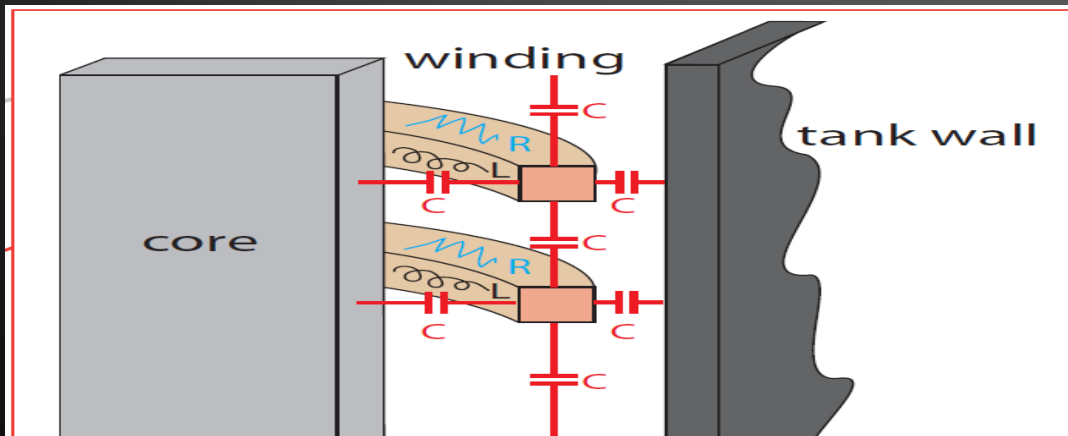
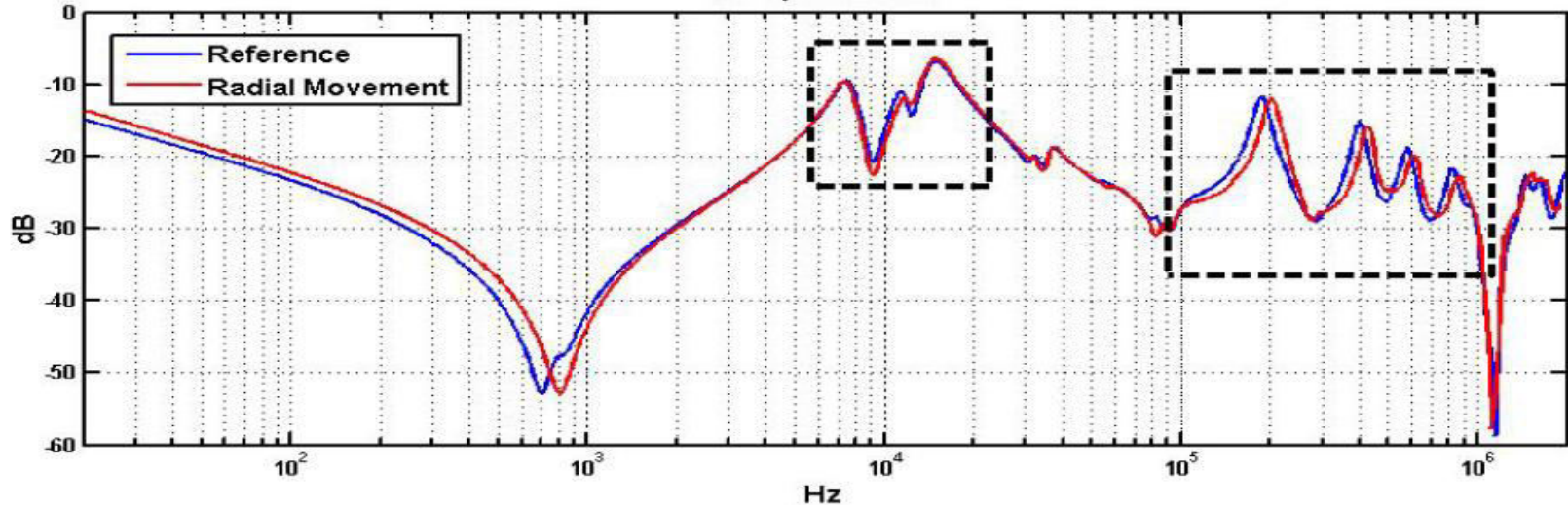


## Answer: FRA

1. Provides prerequisite sensitivity to detect such conditions
2. A mismatch in FRA implies a damage-situation
3. But, currently is limited to detection only
4. Unique interpretation of FRA is not yet possible

# FRA : Working principle

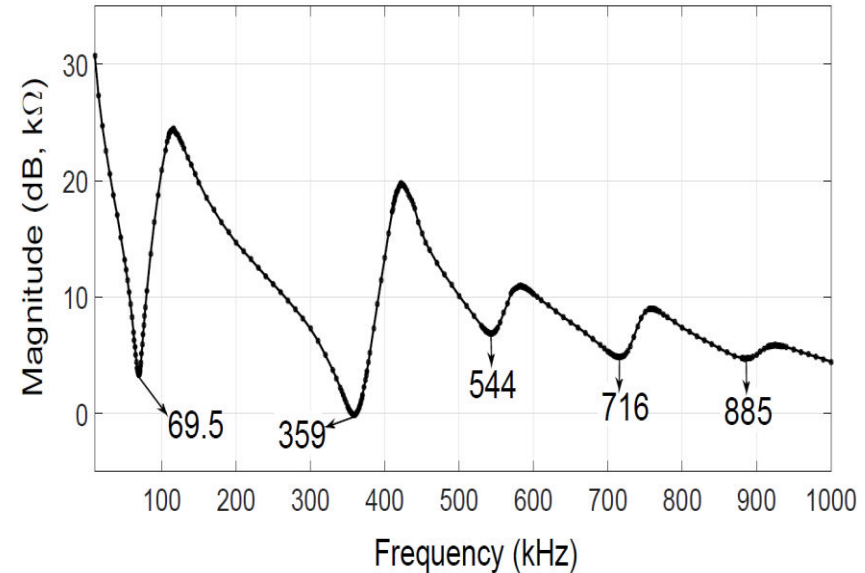
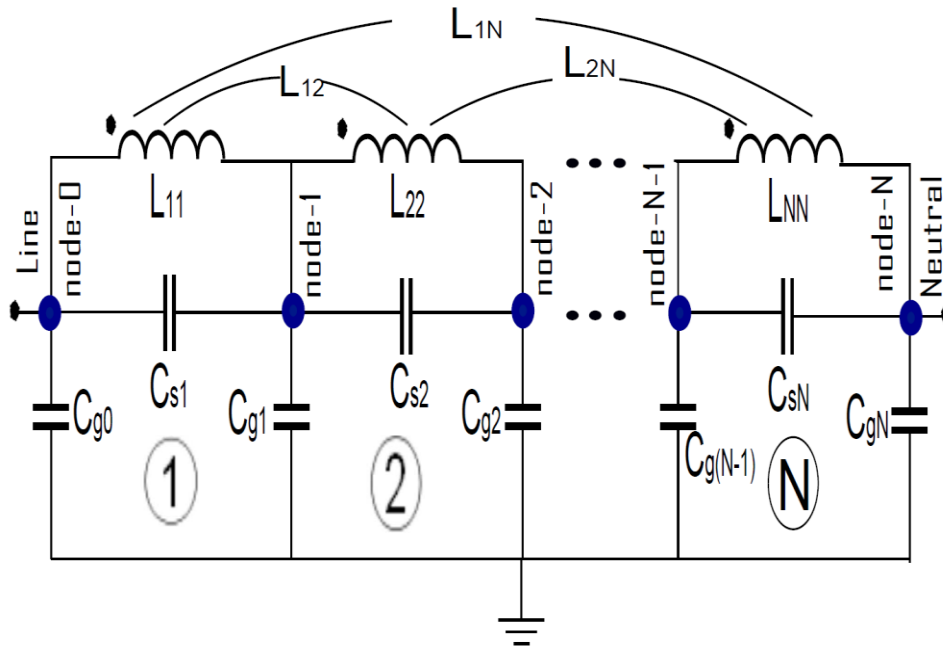
LV Open Circuit



The core-and-winding-assembly of power transformers can be seen as a complex electrical network of capacitances, inductances and resistors.

A mechanical damage in the winding leads to inductance & capacitance changes. This causes a new set of natural frequencies.

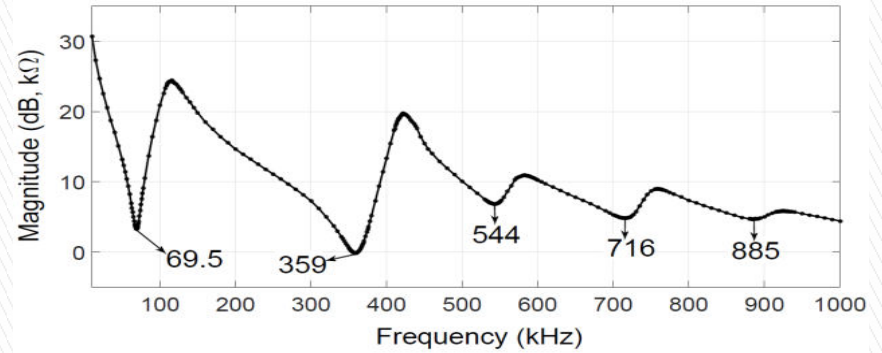
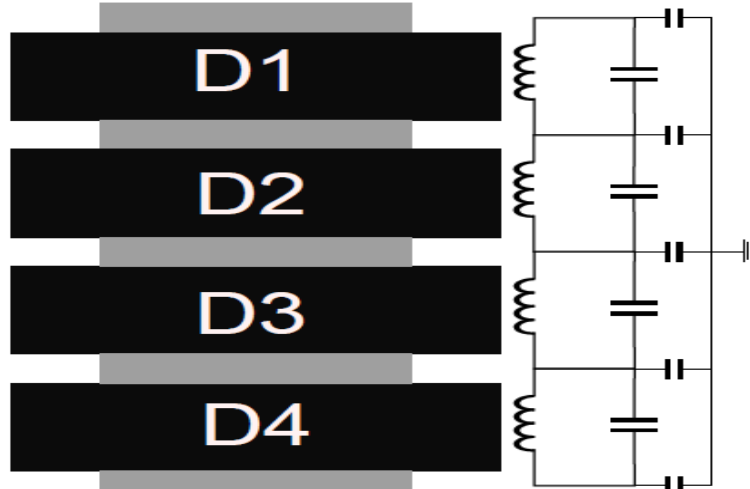
# Analytical correlation linking natural frequency and winding parameters



$$\sum_{i=1}^N \frac{1}{\omega_{SCi}^2} = \sum_{i=1}^N L_{ii} C_{si} + \sum_{i=1}^N M_{0i} C_{gi}$$

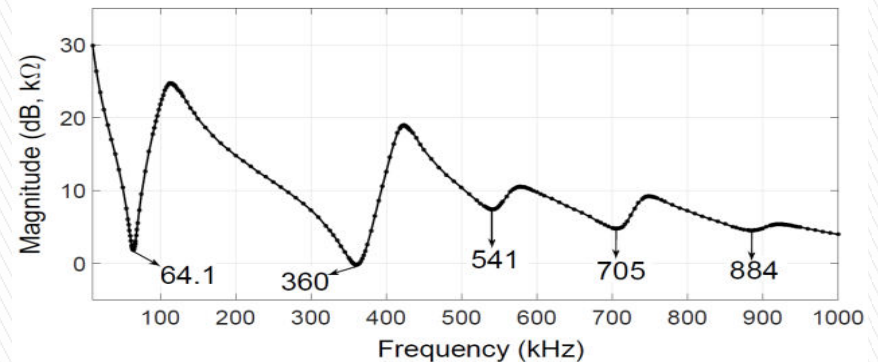
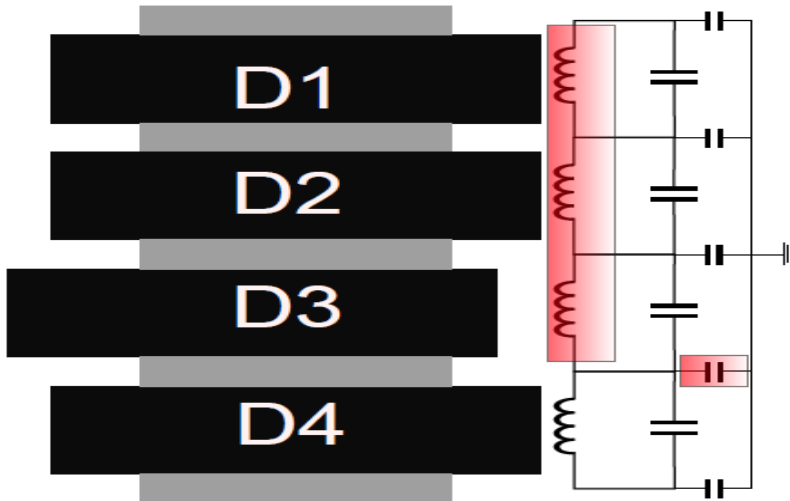


# Radial Displacement Localization



(a) DPI of nominal winding

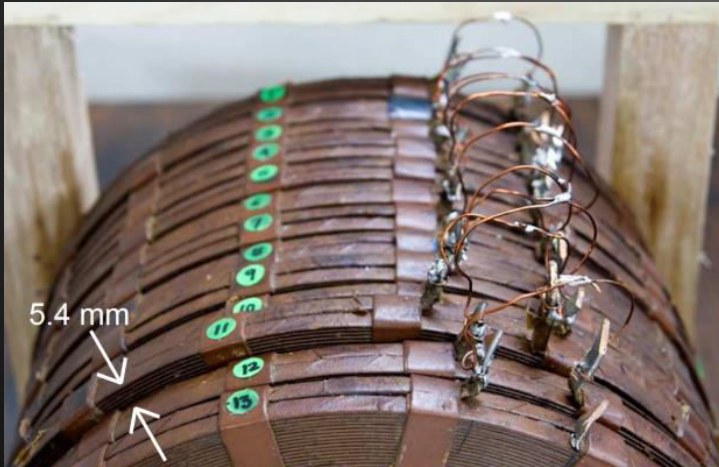
$$\Delta\Psi_{scnf} = \sum 1/\hat{\omega}_{sc_i}^2 - \sum 1/\omega_{sc_i}^2 = M_{03}\Delta C_g$$



(b) DPI of winding after 11<sup>th</sup> is disk-pair radially displaced



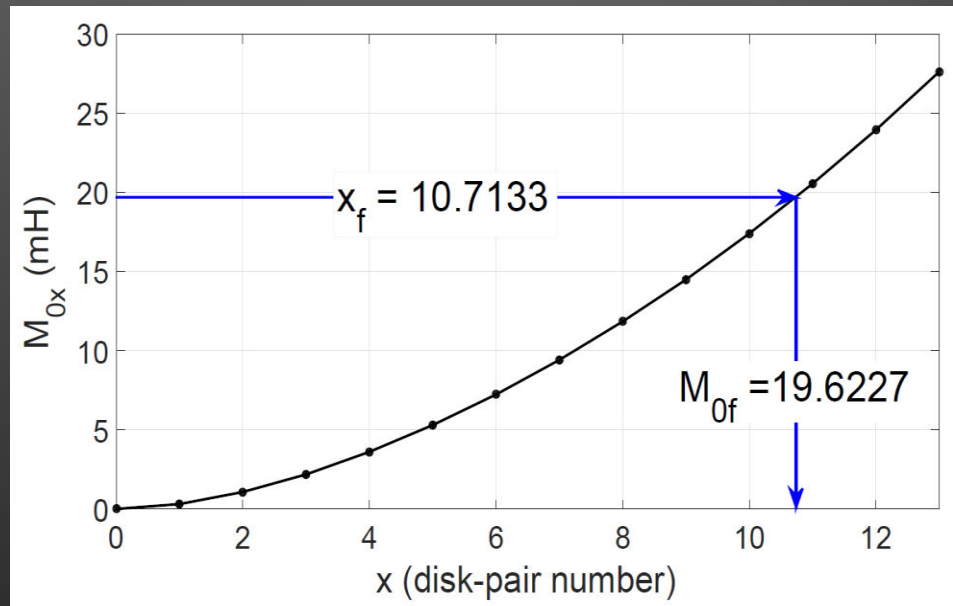
# Result: RD location



$$\begin{aligned}\Delta\Psi_{scnf} &= \widehat{\Psi}_{scnf} - \Psi_{scnf} \\ &= 6.5302 - 5.6080 = 0.9223\end{aligned}$$

$$\Delta C_g = \widehat{C}_G - C_G = 0.047 \text{ nF}$$

$$M_{0f} = \Delta\Psi_{scnf} / \Delta C_g = 19.6227 \text{ mH}$$



# RD: Assessment of Severity

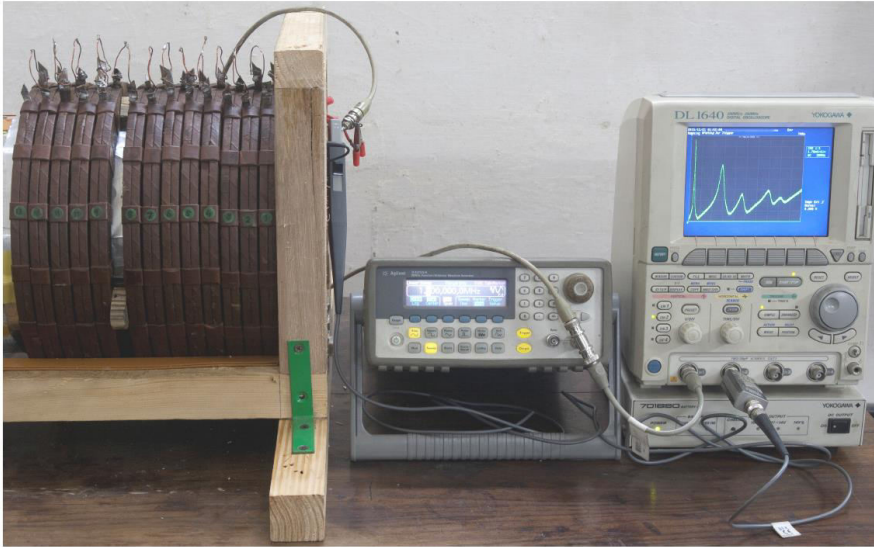


PROPORTIONALITY OF  $\Delta\Psi_{scnf}$  W.R.T. SEVERITY

| Disk pair | extent (mm) | SCNFs (kHz)     |                 |                 |                 |                 | $\Delta\Psi_{scnf}$ |
|-----------|-------------|-----------------|-----------------|-----------------|-----------------|-----------------|---------------------|
|           |             | 1 <sup>st</sup> | 2 <sup>nd</sup> | 3 <sup>rd</sup> | 4 <sup>th</sup> | 5 <sup>th</sup> |                     |
| 4         | 3           | 69.1            | 354             | 536             | 718             | 886             | 0.0687              |
| 4         | 4           | 68.8            | 348             | 531             | 718             | 888             | 0.1236              |
| 4         | 5           | 68.5            | 345             | 529             | 718             | 886             | 0.1751              |
| 7         | 3           | 68.6            | 354             | 548             | 714             | 889             | 0.1428              |
| 7         | 4           | 67.6            | 346             | 547             | 710             | 888             | 0.3137              |
| 7         | 5           | 67.2            | 345             | 548             | 707             | 888             | 0.3812              |
| 10        | 3           | 68              | 362             | 541             | 715             | 889             | 0.2315              |
| 10        | 4           | 66.7            | 361             | 536             | 714             | 889             | 0.4499              |
| 10        | 5           | 65.7            | 361             | 535             | 713             | 888             | 0.6251              |
| 10        | 6           | 63.7            | 359             | 533             | 712             | 886             | 1.0025              |

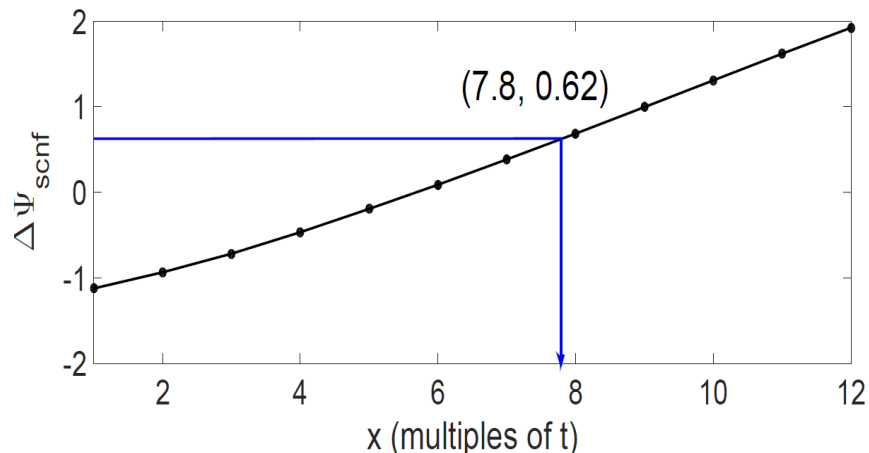


# Axial Displacement

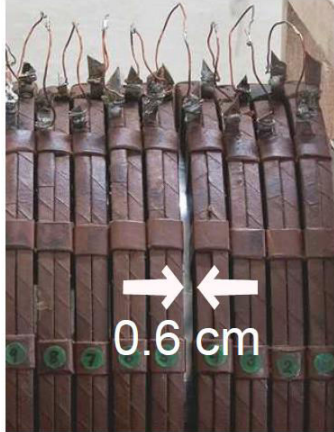


The **monotonic variation of  $\Delta\Psi_{scnf}$**  is the key to localize the change. This property is used for locating and assessing the severity of an RD

An AD involves **a large number of inductance changes as well as capacitance changes**. So, handling AD is more involved. But, monotonicity of  $\Delta\Psi_{scnf}$  can be used to advantage for the task of localization



# AD: varying degree



Performance of the algorithm independent of the location or the extent of AD

Table 4.5: CASE-B: RESULTS FOR AD WITH VARYING EXTENT OF DISPLACEMENT

| Disk pair | Extent of AD (cm) | SCNFs (kHz)     |                 |                 |                 |                 | $\Delta C_g$ (nF) | $\Delta L_{eq}$ (mH) | Location                 | Estimated extent (cm) |
|-----------|-------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-------------------|----------------------|--------------------------|-----------------------|
|           |                   | 1 <sup>st</sup> | 2 <sup>nd</sup> | 3 <sup>rd</sup> | 4 <sup>th</sup> | 5 <sup>th</sup> |                   |                      |                          |                       |
| 4-5       | 0.6               | 42.3            | 283             | 482             | 694             | 862             | 0.047             | -0.55                | 5.7 $\Rightarrow$ D5-D6  | 0.3089t=0.52          |
|           | 1.4               | 42.4            | 278             | 473             | 700             | 845             | 0.075             | -1.03                | 5.9 $\Rightarrow$ D5-D6  | 0.599t=1.01           |
|           | 2.0               | 42.4            | 275             | 470             | 695             | 842             | 0.087             | -1.68                | 5.8 $\Rightarrow$ D5-D6  | 1.026t=1.74           |
| 9-10      | 0.6               | 42.0            | 287             | 477             | 684             | 870             | 0.038             | -0.59                | 8.5 $\Rightarrow$ D8-D9  | 0.3323t=0.56          |
|           | 1.4               | 41.5            | 289             | 461             | 681             | 870             | 0.058             | -1.13                | 9.1 $\Rightarrow$ D9-D10 | 0.7313t=1.24          |
|           | 2.0               | 41.1            | 288             | 455             | 678             | 870             | 0.092             | -1.78                | 8.5 $\Rightarrow$ D8-D9  | 1.0954t=1.85          |

# Conclusions

- ▶ Analytical framework established for FRA diagnosis
- ▶ New relationships derived to correlate winding parameters to natural frequencies
- ▶ RD and AD in an actual winding can be located, its severities can also be assessed
- ▶ Future scope: Existing formulation has to be extended for diagnosis of other types of damages



**Thank you  
for your kind attention**

**Questions?**

